

Introduction to Functional Programming and Clojure

Jan-Willem van de Meent

Anatomy of a Clojure Program

```
(ns examples.factorial
  (:gen-class))

(defn factorial
  "computes n * (n-1) * ... * 1"
  [n]
  (if (= n 1)
      1
      (* n (factorial (- n 1)))))

(defn -main
  [& args]
  (doseq [arg args]
    (let [n (Long/parseLong arg)]
      (println "the factorial of" arg
               "is" (factorial n)))))
```

Anatomy of a Clojure Program

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Namespace
declaration

```
(defn factorial
  "computes n * (n-1) * ... * 1"
  [n]
  (if (= n 1)
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      (* n (factorial (- n 1)))))
```

```
(defn -main
  [& args]
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```

Recursive
function

```
(defn -main  
  [& args]  
  (doseq [arg args]  
    (let [n (Long/parseLong arg)]  
      (println "the factorial of" arg  
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  (doseq [arg args]
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      (println "the factorial of" arg
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Main
function

How do I run this?

```
# get source code for this tutorial  
git clone git@bitbucket.org:probprog/ppaml-summer-school-2016.git  
cd ppaml-summer-school-2016/exercises/
```

```
# option 1: build uberjar and run via java  
lein uberjar  
java -cp target/uberjar/examples-0.1.0-SNAPSHOT.jar \  
  examples.factorial 1 2 5 20
```

```
# option 2: run using Leiningen  
lein run -m examples.factorial 1 2 5 20
```

```
# => the factorial of 1 is 1  
# => the factorial of 2 is 2  
# => the factorial of 5 is 120  
# => the factorial of 20 is 2432902008176640000
```

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option 2: run using Leiningen

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=> the factorial of 1 is 1

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=> the factorial of 1 is 1

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# => the factorial of 1 is 1
```

```
# => the factorial of 2 is 2
```

```
# => the factorial of 5 is 120
```

```
# => the factorial of 20 is 2432902008176640000
```

Interactive Shell: the REPL

```
$ lein repl
# => nREPL server started on port 50240 on host
      127.0.0.1 - nrepl://127.0.0.1:50240
# => REPL-y 0.3.7, nREPL 0.2.12
# => Clojure 1.8.0
# => Java HotSpot(TM) 64-Bit Server VM 1.8.0-b132
# =>      Docs: (doc function-name-here)
# =>           (find-doc "part-of-name-here")
# =>      Source: (source function-name-here)
# =>      Javadoc: (javadoc java-object-or-class-here)
# =>      Exit: Control+D or (exit) or (quit)
# =>      Results: Stored in vars *1, *2, *3,
                  an exception in *e
```

```
examples.core=>
```

Interactive Shell: the REPL

```
examples.core=> (require 'examples.factorial)
;; => nil
```

```
examples.core=> (ns 'examples.factorial)
;; => #object[clojure.Lang.Namespace 0x42cd2abe
"examples.factorial"]
```

```
examples.factorial=> (-main "1" "2" "5" "20")
;; => the factorial of 1 is 1
;; => the factorial of 2 is 2
;; => the factorial of 5 is 120
;; => the factorial of 20 is 2432902008176640000
;; => nil
```

Gorilla REPL

```
$ lein gorilla
```



The screenshot shows a web browser window titled "Gorilla REPL - exercises" with the address bar displaying "127.0.0.1:62175/worksheet.html". The interface contains two code blocks, each with a text input area below it. The first code block contains the code `(ns hello-world (:require [examples.factorial]))` and its output is `nil`. The second code block contains the code `(examples.factorial/-main "1" "2" "5" "10")` and its output is `the factorial of 1 is 1`, `the factorial of 2 is 2`, `the factorial of 5 is 120`, and `the factorial of 10 is 3628800`. The output of the second code block is highlighted with a pink border. A hamburger menu icon is visible in the top right corner of the interface.

```
(ns hello-world
  (:require [examples.factorial]))
```

```
nil
```

```
(examples.factorial/-main "1" "2" "5" "10")
```

```
the factorial of 1 is 1
the factorial of 2 is 2
the factorial of 5 is 120
the factorial of 10 is 3628800
```

```
nil
```

Anatomy of a Clojure Function

```
(ns examples.factorial
  (:gen-class))

(defn factorial
  "computes n * (n-1) * ... * 1"
  [n]
  (if (= n 1)
      1
      (* n (factorial (- n 1)))))

(defn -main
  [& args]
  (doseq [arg args]
    (let [n (Long/parseLong arg)]
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(defn factorial
  "computes n * (n-1) * ... * 1"
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```

```
def factorial(n):
    '''computes n * (n - 1) * ... * 1'''
    if n == 1:
        return 1
    else:
        return n * factorial(n - 1)
```

Anatomy of a Clojure Function

```
(defn factorial  
  "computes n * (n-1) * ... * 1"  
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```

Name

```
def factorial(n):  
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Anatomy of a Clojure Function

```
(defn factorial  
  "computes n * (n-1) * ... * 1"  
  [n]  
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```

Docstring

```
def factorial(n):  
    '''computes n * (n - 1) * ... * 1'''  
    if n == 1:  
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Anatomy of a Clojure Function

```
(defn factorial
  "computes n * (n-1) * ... * 1"
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Arguments

```
def factorial(n):
    '''computes n * (n - 1) * ... * 1'''
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        return 1
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Anatomy of a Clojure Function

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(defn factorial
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Function
body

```
def factorial(n):
    '''computes n * (n - 1) * ... * 1'''
    if n == 1:
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Anatomy of a Clojure Function

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S-expression

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def factorial(n):
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Block
statement

Anatomy of an Expression

```
(defn factorial  
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Anatomy of an Expression

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expression ::= symbol | literal | (operator ...)

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Data Types

Atomic

;; symbols
(`symbol` "ada"), ada

;; keywords
`:ada`

;; integers, doubles, ratios
1234, 1.234, 12/34

;; strings, characters
`"ada"`, `\a \d \a`

;; booleans, null
true, false, nil

;; regular expressions
`#"a*b"`

Collections

;; lists
(`list` 1 2 3), (1 2 3)

;; hash maps
{`:a` 1 `:b` 2}

;; vectors
[1 2 3]

;; sets
`#{1 2 3}`

;; everything nests
{`:a` [[1 2] [3 4]]
 `:b` `#{5 6 (list 7 8)}`
 `:c` {"d" 9 `\e` 10}}

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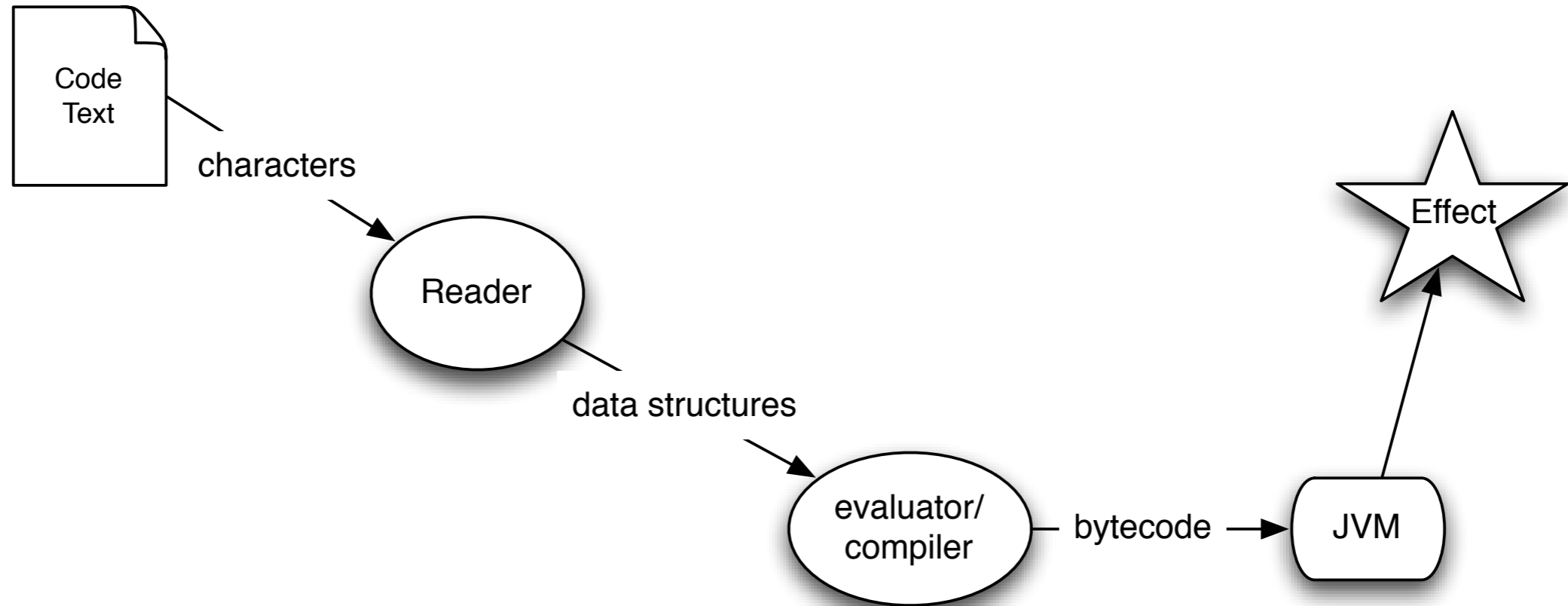
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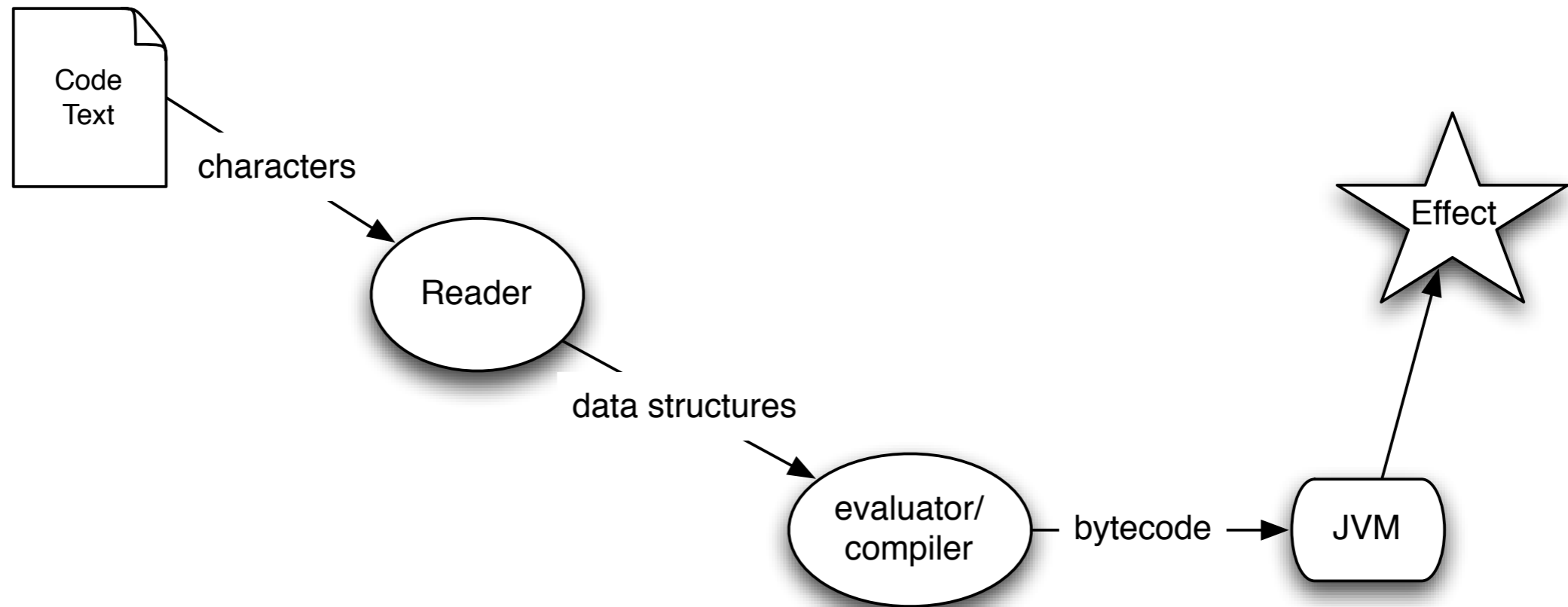
Evaluation in Clojure



```
(let [expr (read-string "(+ 1 2)")]  
  (prn expr) ; => (+ 1 2)  
  (prn (class expr)) ; => clojure.lang.PersistentList  
  (prn (class (first expr))) ; => clojure.lang.Symbol  
  (eval expr)) ; => 3
```

(image credit: Rich Hickey)

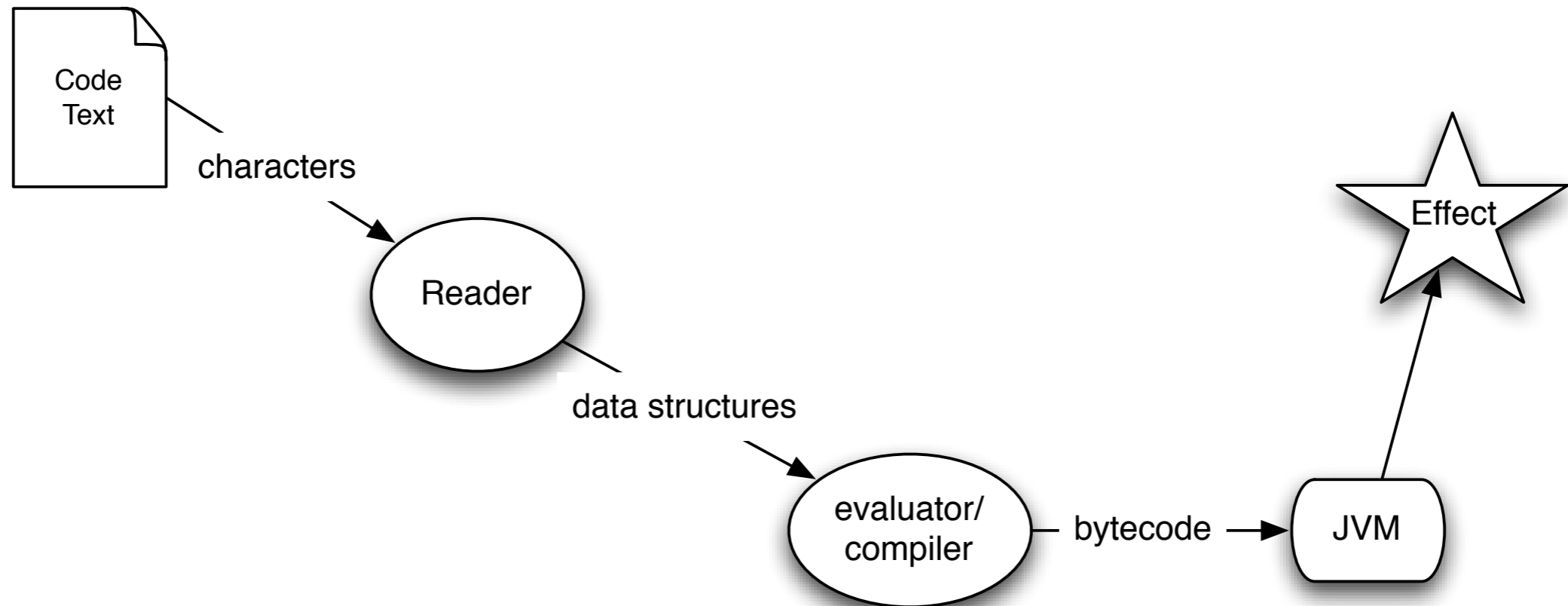
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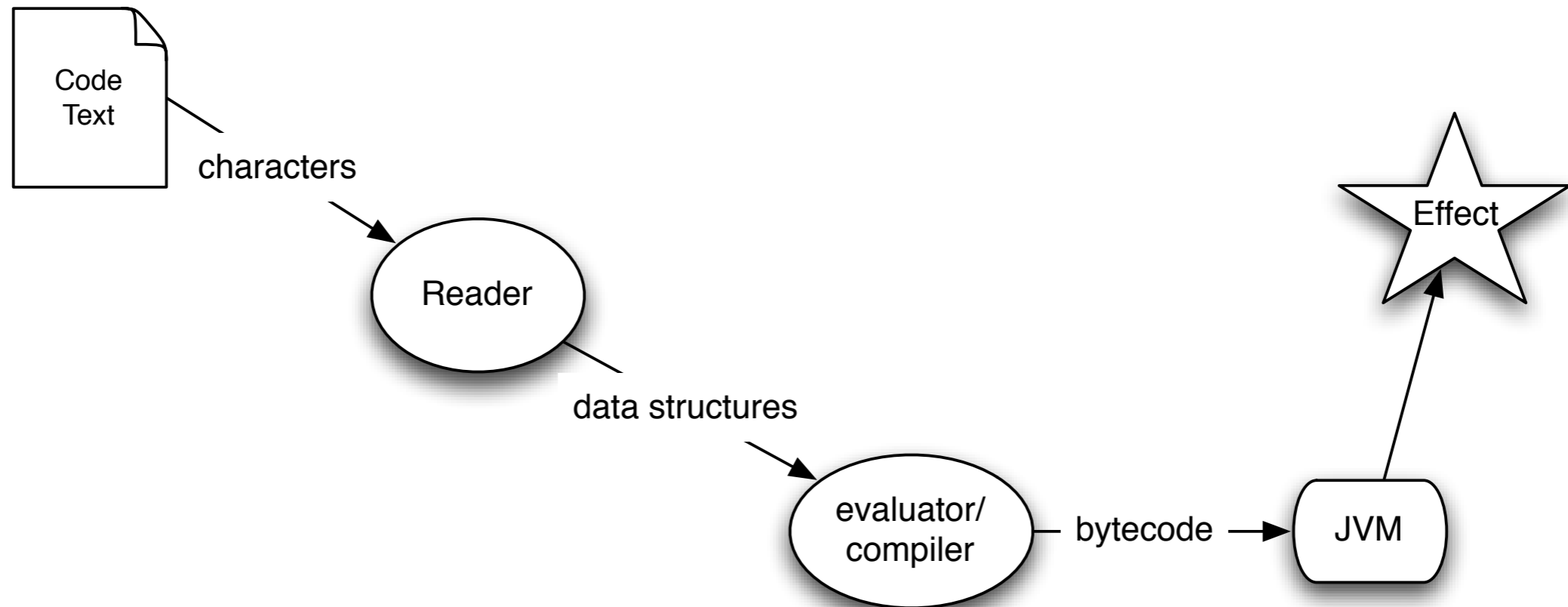
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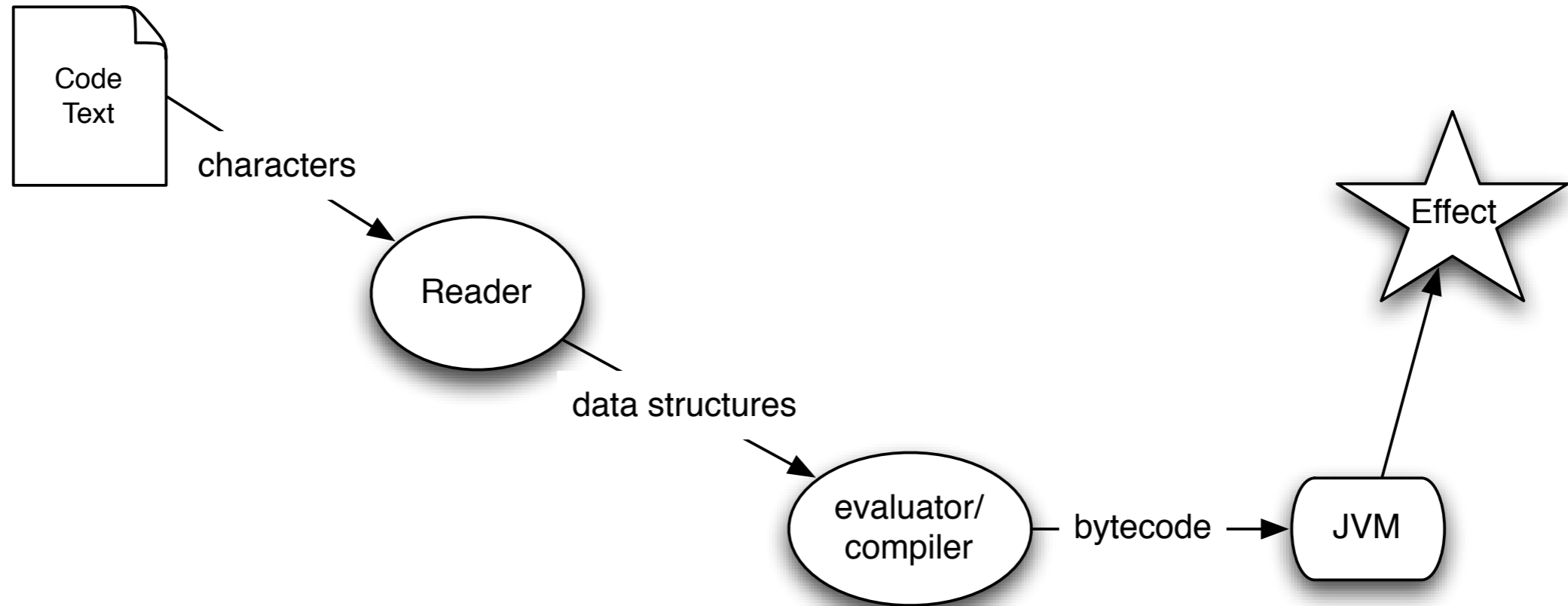
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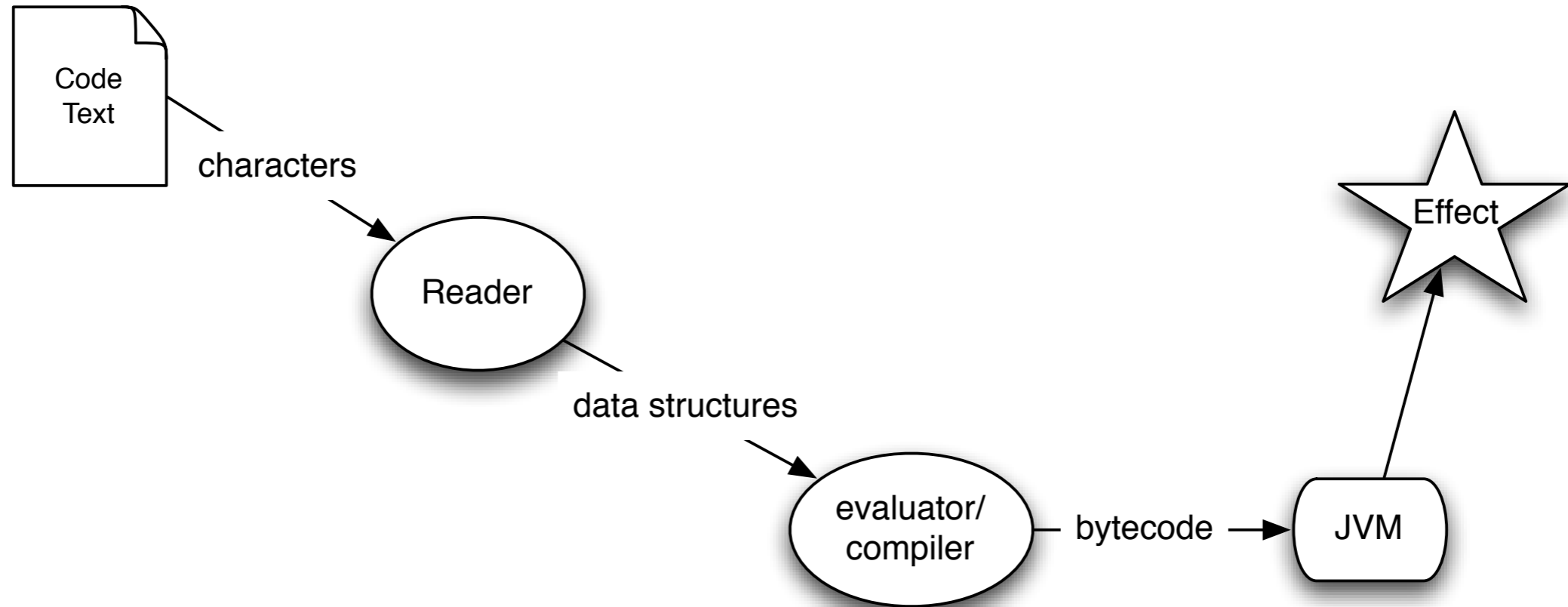
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(let [expr (read-string "(+ 1 2)")]  
  (prn expr) ; => (+ 1 2)  
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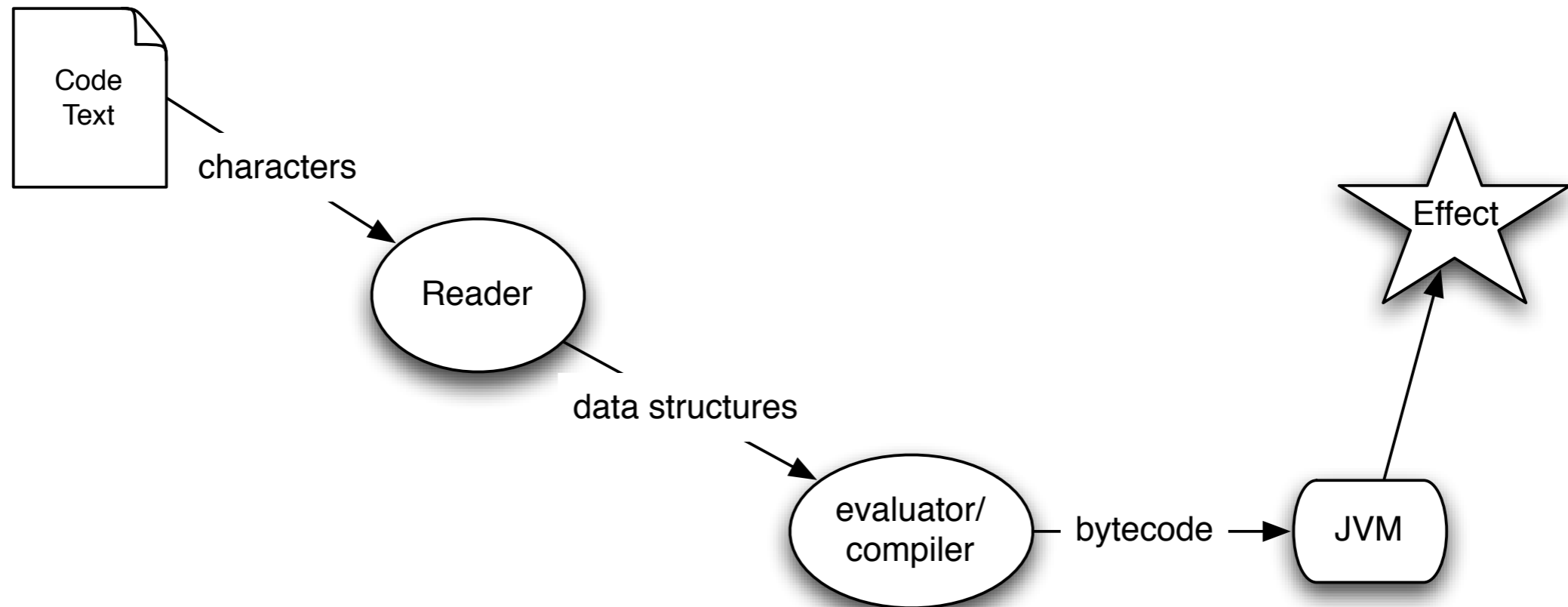
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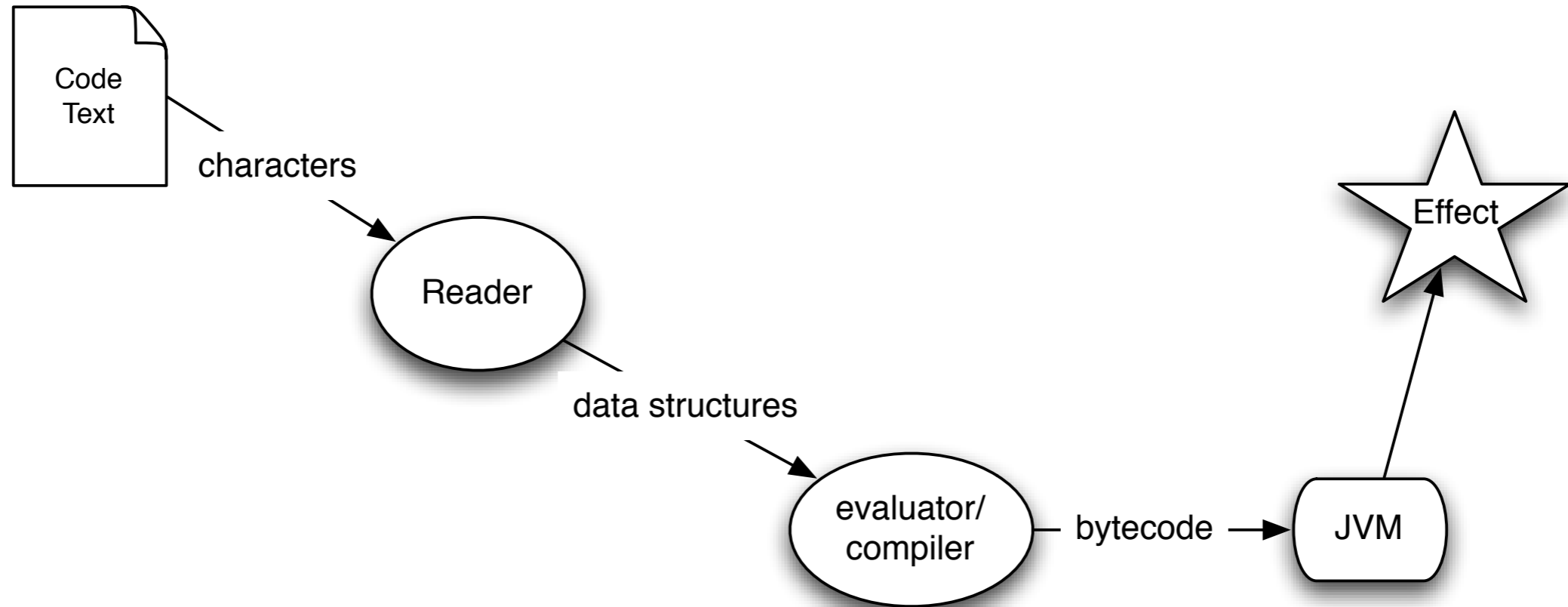
Evaluation in Clojure



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  (prn expr) ; => (+ 1 2)  
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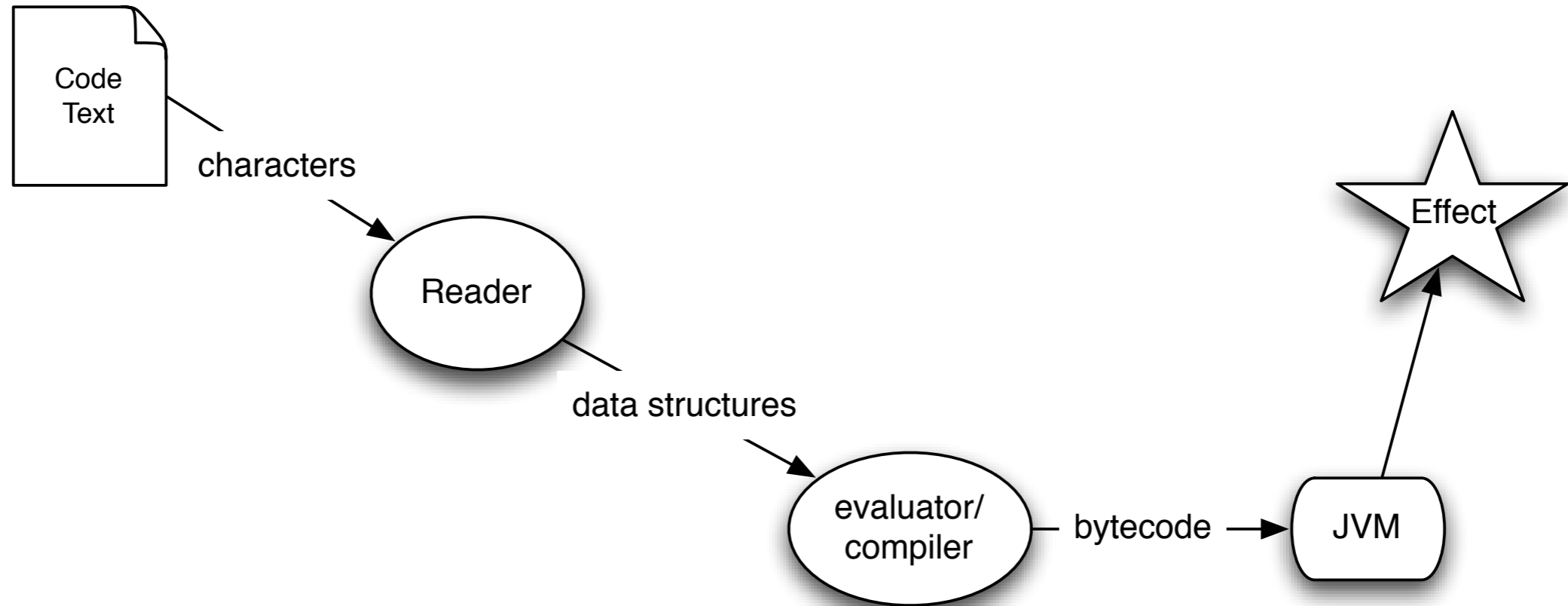
Evaluation in Clojure



```
(let [expr '(+ 1 2)]  
  (prn expr) ; => (+ 1 2)  
  (prn (class expr)) ; => clojure.lang.PersistentList  
  (prn (class (first expr))) ; => clojure.lang.Symbol  
  (eval expr)) ; => 6
```

(image credit: Rich Hickey)

Evaluation in Clojure



```
(let [expr (quote (+ 1 2))]  
  (prn expr) ; => (+ 1 2)  
  (prn (class expr)) ; => clojure.lang.PersistentList  
  (prn (class (first expr))) ; => clojure.lang.Symbol  
  (eval expr)) ; => 6
```

(image credit: Rich Hickey)

Macros

```
(defmacro unless
  "Inverted 'if"
  [pred then else]
  (list 'if pred else then))
```

```
(def flavor :tasty)
```

```
(unless (= flavor :tasty)
  :yuk
  :yum)
```

; ~> *(macro-expansion)*

```
(if (= flavor :tasty)
  :yum
  :yuk)
```

; => *(evaluation)*

```
:yum
```


Looping

```
(defn factorial
  "computes n * (n-1) * ... * 1"
  [n]
  (if (= n 1)
      1
      (* n (factorial (- n 1)))))
```

Looping

```
(defn factorial
  "computes n * (n-1) * ... * 1"
  [n]
  (if (= n 1)
      1
      (* n (factorial (- n 1)))))
```

```
(factorial 21)
; => ArithmeticException integer overflow
;   clojure.lang.Numbers.throwIntOverflow (Numbers.java:1501)
```

Looping

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(defn factorial
  "computes n * (n-1) * ... * 1"
  [n]
  (if (= n 1)
      1N
      (* n (factorial (- n 1)))))
```

```
(factorial 21)
; => ArithmeticException integer overflow
;   clojure.lang.Numbers.throwIntOverflow (Numbers.java:1501)
```

Looping

```
(defn factorial
  "computes n * (n-1) * ... * 1"
  [n]
  (if (= n 1)
      1
      (* n (factorial (- n 1)))))
```

```
(factorial 21)
; => ArithmeticException integer overflow
;   clojure.lang.Numbers.throwIntOverflow (Numbers.java:1501)
```

Looping

```
(defn factorial
  "computes n * (n-1) * ... * 1"
  [n]
  (if (= n 1)
      1
      (* n (factorial (- n 1)))))
```

```
(factorial 10000)
; => StackOverflowError
      clojure.lang.Numbers.equal (Numbers.java:216)
```

Looping

```
(defn factorial
  "computes n * (n-1) * ... * 1"
  [n]
  (if (= n 1)
      1
      (* n (factorial (- n 1)))))
```

```
def factorial(n):
    '''computes n * (n - 1) * ... * 1'''
    if n == 1:
        return 1
    else:
        return n * factorial(n - 1)
```

Looping

```
(defn
```

```
[
```

```
(
```

```
(
```

```
def factorial(n):  
    '''computes n * (n - 1) * ... * 1'''  
    result = 1  
    for i in range(2, n + 1):  
        result *= i  
    return result
```

Looping

```
(defn
```

```
[
```

```
(
```

```
(
```

```
def factorial(n):  
    '''computes n * (n - 1) * ... * 1'''  
    result = 1  
    ivals = range(2, n + 1)  
    while ivals:  
        i = ivals.pop(0)  
        result *= i  
    return result
```


Looping

```
(defn factorial [n]
  "computes n * (n-1) * ... * 1"
  (loop [result 1
        ivals (range 2 (+ n 1))]
    (if (seq ivals)
        (recur (*' result (first ivals))
              (rest ivals))
        result)))
```

def

result
ivals

i
result

Looping

```
(defn factorial [n]
  "computes n * (n-1) * ... * 1"
  (loop [result 1
        ivals (range 2 (+ n 1))]
    (if (seq ivals)
        (recur (*' result (first ivals))
              (rest ivals))
        result)))
```

Start loop

def

```
result
ivals
```

```
  i
  result
```

Looping

```
(defn factorial [n]
  "computes n * (n-1) * ... * 1"
  (loop [result 1
        ivals (range 2 (+ n 1))]
    (if (seq ivals)
        (recur (*' result (first ivals))
              (rest ivals))
        result)))
```

Initial values

def

result
ivals

i
result

Looping

```
(defn factorial [n]
  "computes n * (n-1) * ... * 1"
  (loop [result 1
        ivals (range 2 (+ n 1))]
    (if (seq ivals)
        (recur (*' result (first ivals))
               (rest ivals))
        result)))
```

Any values
for **i** remaining?

def

result
ivals

i
result

Looping

```
(defn factorial [n]
  "computes n * (n-1) * ... * 1"
  (loop [result 1
        ivals (range 2 (+ n 1))]
    (if (seq ivals)
        (recur (*' result (first ivals))
               (rest ivals))
        result)))
```

Compute values
for next iteration

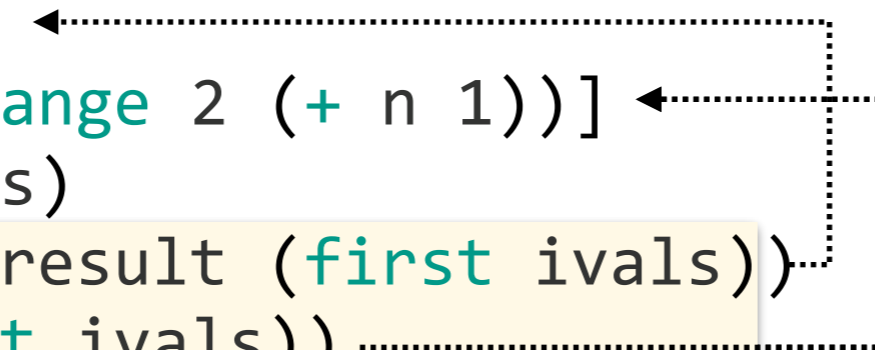
def

result
ivals

i
result

Looping

```
(defn factorial [n]
  "computes n * (n-1) * ... * 1"
  (loop [result 1
        ivals (range 2 (+ n 1))]
    (if (seq ivals)
      (recur (* result (first ivals))
             (rest ivals))
      result)))
```



Compute values
for next iteration

def

result
ivals

i
result

Looping

```
(defn factorial [n]
  "computes n * (n-1) * ... * 1"
  (loop [result 1
        ivals (range 2 (+ n 1))]
    (if (seq ivals)
        (recur (*' result (first ivals))
               (rest ivals))
        result)))
```

Output

def

result

ivals

i

result

Looping

```
(defn factorial [n]
  "computes n * (n-1) * ... * 1"
  (loop [result 1
        ivals (range 2 (+ n 1))]
    (if (seq ivals)
        (recur (*' result (first ivals))
              (rest ivals))
        result)))
```

def

result
ivals

i
result

Looping

```
(defn factorial [n]
  "computes n * (n-1) * ... * 1"
  (loop [result 1
        ivals (range 2 (+ n 1))]
    (if (seq ivals)
        (recur (*' result (first ivals))
               (rest ivals))
        result)))
```

```
def factorial(n):
    '''computes n * (n - 1) * ... * 1'''
    result = 1
    ivals = range(2, n + 1)
    while ivals:
        i = ivals.pop(0)
        result *= i
    return result
```

Looping

```
(defn factorial [n]
  "computes n * (n-1) * ... * 1"
  (loop [result 1
        ivals (range 2 (+ n 1))]
    (if (seq ivals)
        (recur (*' result (first ivals))
              (rest ivals))
        result)))
```

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def factorial(n):
    '''computes n * (n - 1) * ... * 1'''
    result = 1
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    while ivals:
        i = ivals.pop(0)
        result *= i
    return result
```

Looping

```
(defn factorial [n]
  "computes n * (n-1) * ... * 1"
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        ivals (range 2 (+ n 1))]
    (if (seq ivals)
        (recur (*' result (first ivals))
              (rest ivals))
        result)))
```

```
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    '''computes n * (n - 1) * ... * 1'''
    result = 1
    ivals = range(2, n + 1)
    while ivals:
        i = ivals.pop(0)
        result *= i
    return result
```

Looping

```
(defn factorial [n]
  "computes n * (n-1) * ... * 1"
  (loop [result 1
        ivals (range 2 (+ n 1))]
    (if (seq ivals)
      (recur (*' result (first ivals))
            (rest ivals))
      result)))
```

Passed by value
to next iteration

```
def factorial(n):
    '''computes n * (n - 1) * ... * 1'''
    result = 1
    ivals = range(2, n + 1)
    while ivals:
        i = ivals.pop(0)
        result *= i
    return result
```

Mutated in place

Looping

```
(defn factorial [n]
  "computes n * (n-1) * ... * 1"
  (loop [result 1
        ivals (range 2 (+ n 1))]
    (if (seq ivals)
        (recur (*' result (first ivals))
               (rest ivals))
        result)))
```

```
(factorial 10000)
; => 40238726007709377354370243392300398571937486421071463
;    25437999104299385123986290205920442084869694048004799
;    88610197196058631666872994808558901323829669944590997
;    ...
```

Looping

```
(defn factorial [n]
  "computes n * (n-1) * ... * 1"
  (loop [result 1
        ivals (range 2 (+ n 1))]
    (if (seq ivals)
        (recur (*' result (first ivals))
              (rest ivals))
        result)))
```

Can split into
separate function

```
(factorial 10000)
; => 40238726007709377354370243392300398571937486421071463
;    25437999104299385123986290205920442084869694048004799
;    88610197196058631666872994808558901323829669944590997
;    ...
```

Looping

```
(defn flop  
  "inner loop for factorial"  
  [result ivals]  
  (if (seq ivals)  
      (flop (*' result (first ivals))  
            (rest ivals))  
      result))
```

```
(defn factorial [n]  
  "computes n * (n-1) * ... * 1"  
  (flop 1  
        (range 2 (+ n 1))))
```

Looping

```
(defn flop  
  "inner loop for factorial"  
  [result ivals]  
  (if (seq ivals)  
      (flop (* result (first ivals))  
            (rest ivals))  
      result))
```

```
(defn factorial [n]  
  "computes n * (n-1) * ... * 1"  
  (flop 1  
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```

```
(factorial 10000)  
; => StackOverflowError  
;   clojure.lang.Numbers.equal (Numbers.java:216)
```


Looping

```
(defn floop
  "inner loop for factorial"
  [result ivals]
  (if (seq ivals)
      (floop (*' result (first ivals))
             (rest ivals))
      result))
```

Tail call

```
(defn factorial [n]
  "computes n * (n-1) * ... * 1"
  (floop 1
        (range 2 (+ n 1))))
```

Looping

```
(defn floop
  "inner loop for factorial"
  [result ival]
  (if (seq ival)
      (recur (* result (first ival))
             (rest ival))
      result))
```

recur allows tail
call optimization

```
(defn factorial [n]
  "computes n * (n-1) * ... * 1"
  (floop 1
         (range 2 (+ n 1))))
```

Looping

```
(defn flop
  "inner loop for factorial"
  [result ivals]
  (if (seq ivals)
      (recur (* result (first ivals))
             (rest ivals))
      result))
```

recur allows tail
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```
(defn factorial [n]
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;    88610197196058631666872994808558901323829669944590997
;    ...
```

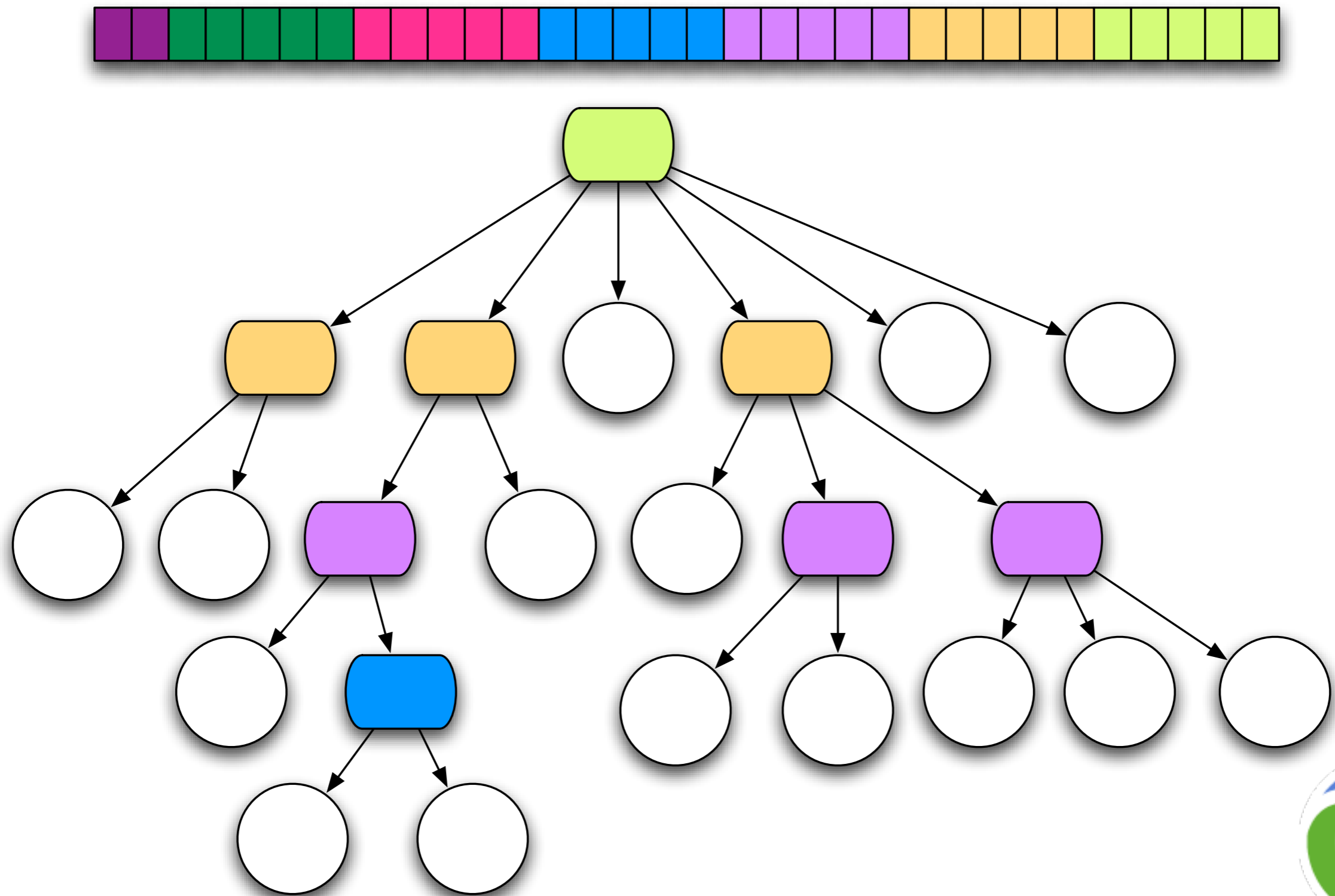
Looping

```
(defn factorial [n]
  "computes n * (n-1) * ... * 1"
  (loop [result 1
        ivals (range 2 (+ n 1))]
    (if (seq ivals)
        (recur (*' result (first ivals))
              (rest ivals))
        result)))
```

Looping

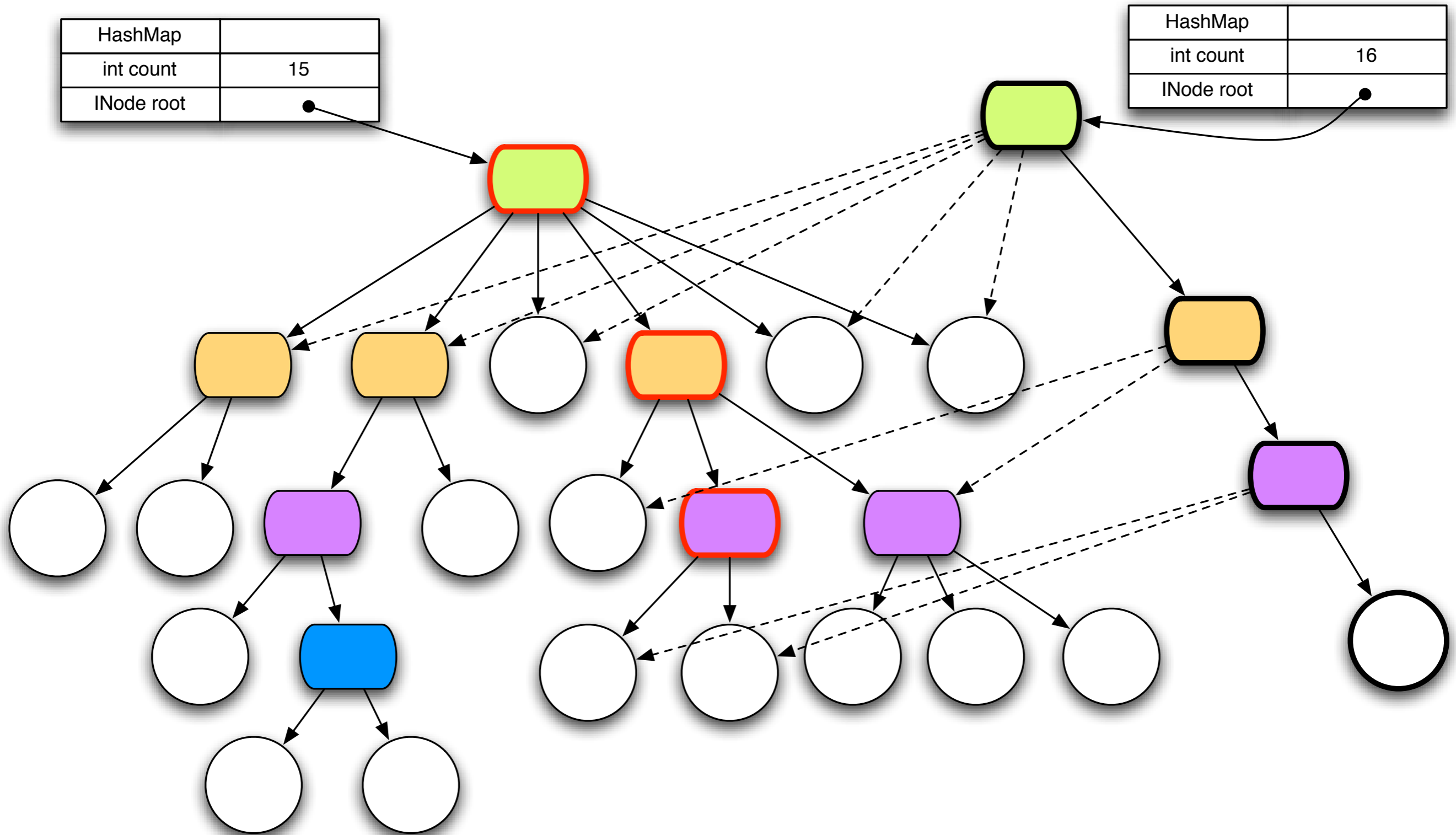
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  "computes n * (n-1) * ... * 1"
  (loop [result 1
        ivals (range 2 (+ n 1))]
    (if (seq ivals)
        (recur (*' result (first ivals))
               (rest ivals))
        result)))
```

Bit-partitioned Hash Tries



(image credit: Rich Hickey)

Path Copying



(image credit: Rich Hickey)

Macros

```
(defmacro dbg
  "Prints an expression and
  its value for debugging."
  [expr]
  (list 'do
    (list 'println
      "[dbg]"
      (list 'quote expr)
      expr)
    expr))
```

```
(dbg (+ 1 2))
; => [dbg] (+ 1 2) 3
; => 3

(macroexpand '(dbg (+ 1 2)))
; => (do
;     (println "[dbg]"
;              (quote (+ 1 2))
;              (+ 1 2))
;     (+ 1 2))
```


Macros

```
(defmacro dbg
  "Prints an expression and
  its value for debugging."
  [expr]
  `(let [value# ~expr]
      (println "[dbg]"
               '~expr
               value#)
      value#))
```

```
(dbg (+ 1 2))
; => [dbg] (+ 1 2) 3
; => 3

(macroexpand '(dbg (+ 1 2)))
; => (let* [value__23707__auto__
            (+ 1 2)]
      (clojure.core/println
       "[dbg]"
       (quote (+ 1 2))
       value__23707__auto__)
      value__23707__auto__)
```